

Outline

- Probabilities
- Bayes' rule (Applied in different fields, including NLP)
- Build your own Naive-Bayes tweet classifier!

Introduction

Corpus of tweets

| | | | | |
|--|--|----------|--|--|
| | | | | |
| | | Positive | | |
| | | | | |
| | | | | |

Introduction

Corpus of tweets

| | | | | |
|--|--|----------|--|--|
| | | | | |
| | | Positive | | |
| | | | | |
| | | | | |
| | | Negative | | |

Tweets containing the word
"happy"

| | | | | |
|--|--|----------|--|--|
| | | | | |
| | | Positive | | |
| | | "happy" | | |
| | | Negative | | |

Probabilities

Corpus of tweets

| | | | | |
|--|--|----------|--|--|
| | | | | |
| | | Positive | | |
| | | | | |
| | | Negative | | |

$A \rightarrow$ Positive tweet

$$P(A) = P(\text{Positive}) = N_{\text{pos}} / N$$

Probabilities

Corpus of tweets

| | | | | |
|--|--|----------|--|--|
| | | | | |
| | | Positive | | |
| | | | | |
| | | Negative | | |

$A \rightarrow$ Positive tweet

$$P(A) = N_{\text{pos}} / N = 13 / 20 = 0.65$$

$$P(\text{Negative}) = 1 - P(\text{Positive}) = 0.35$$

Probabilities

Tweets containing the word
"happy"

| | | | | |
|--|--|--|--|--|
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |

$B \rightarrow$ tweet contains "happy".

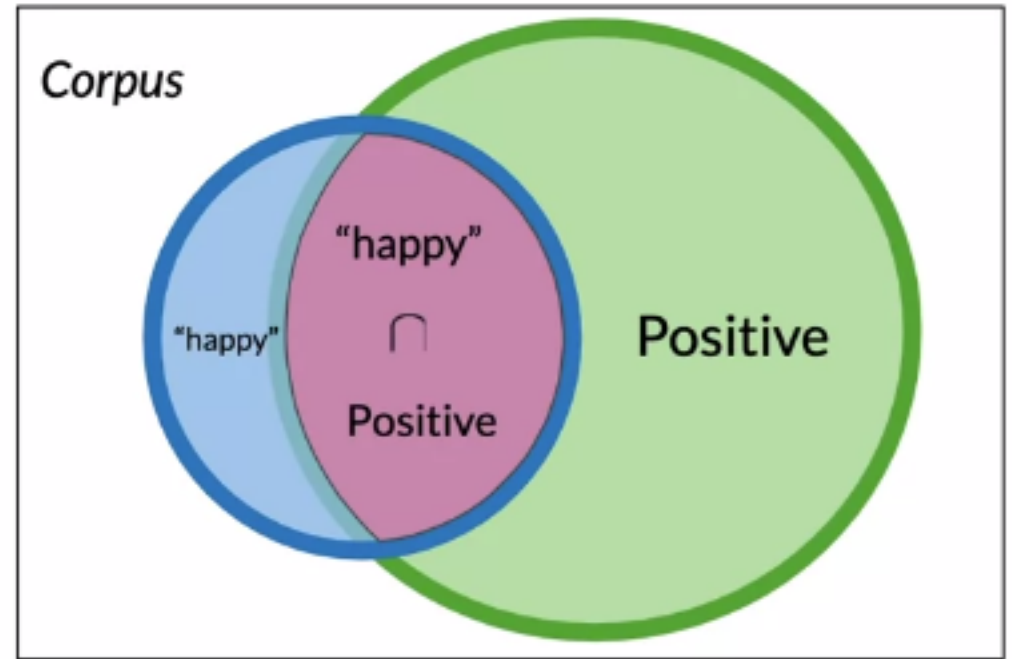
$$P(B) = P(\text{happy}) = N_{\text{happy}} / N$$

$$P(B) = 4 / 20 = 0.2$$

Probability of the intersection

Positive

“happy”



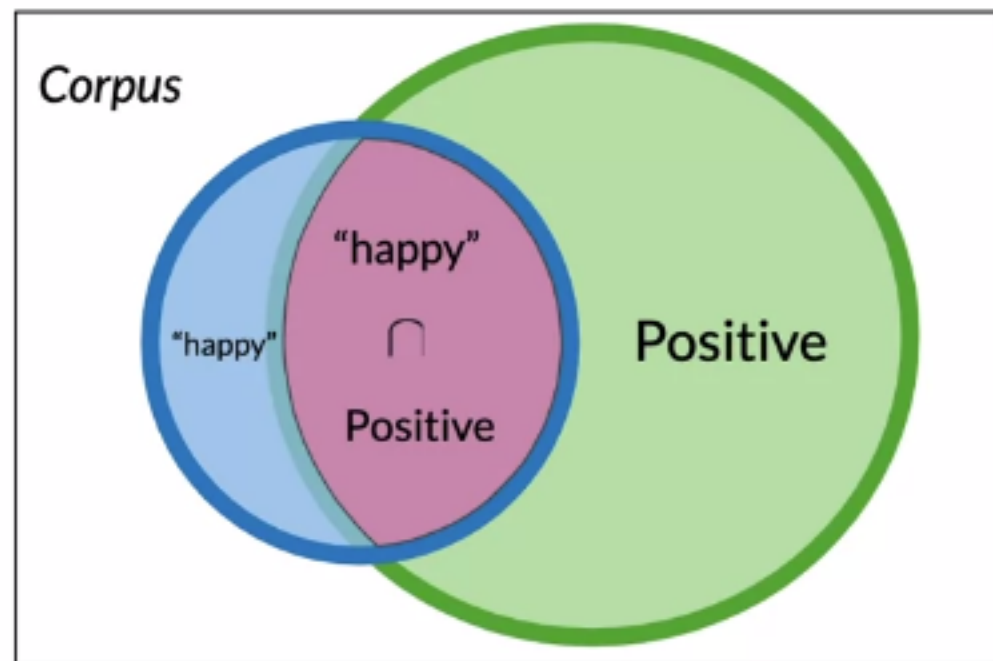
Probability of the intersection



Positive

“happy”

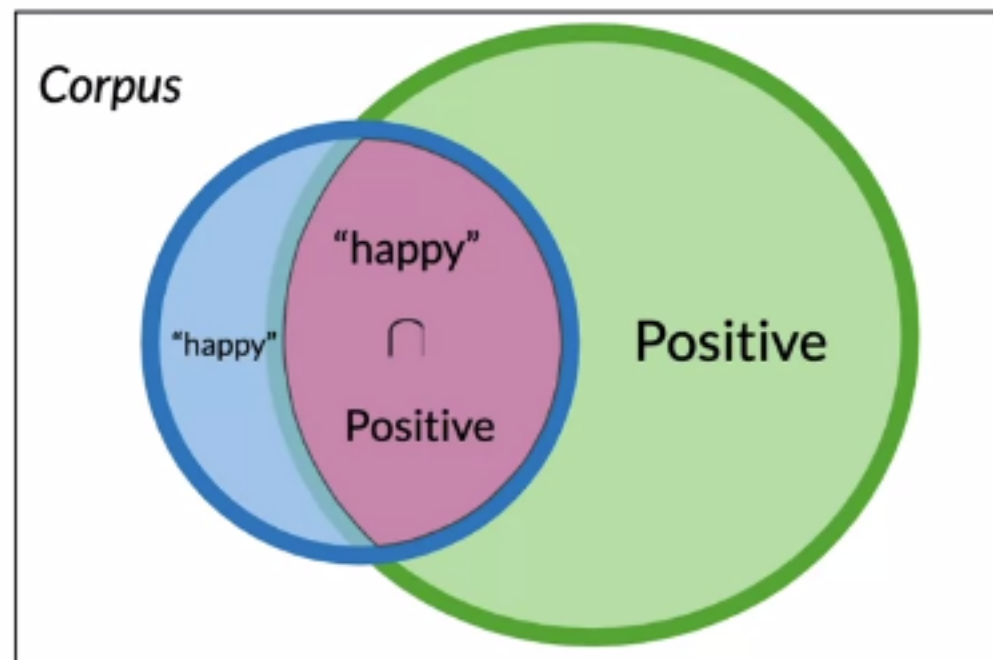
$$P(A \cap B) = P(A, B) =$$



Probability of the intersection



$$P(A \cap B) = P(A, B) = \frac{3}{20} = 0.15$$

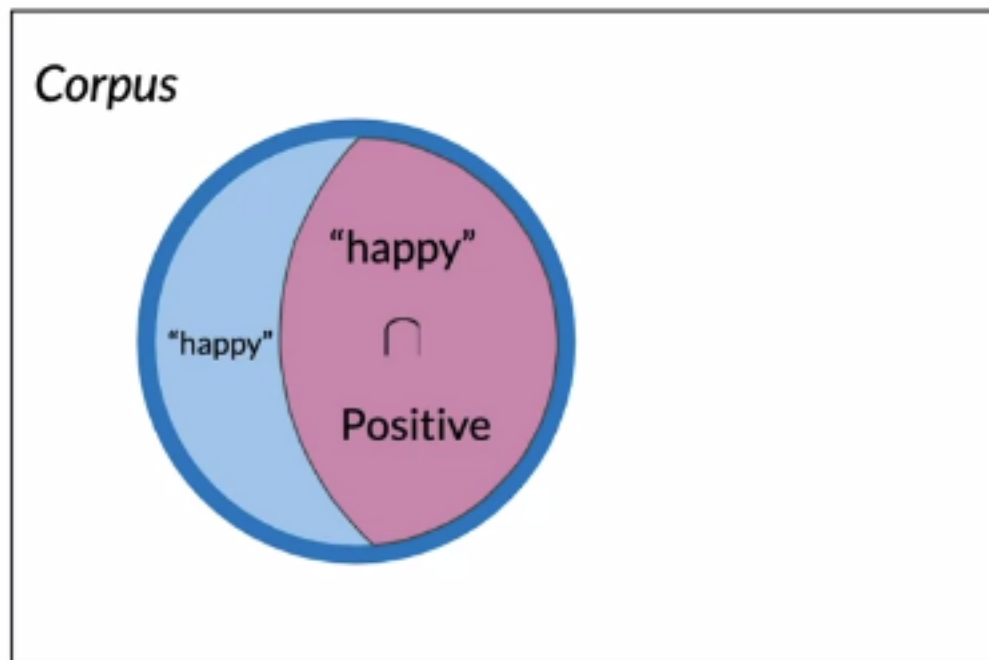
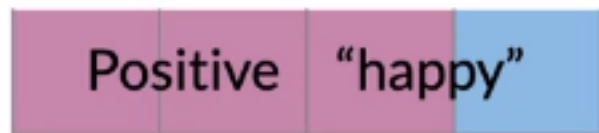




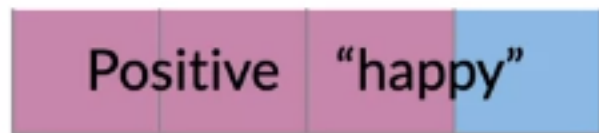
deeplearning.ai

Bayes' Rule

Conditional Probabilities

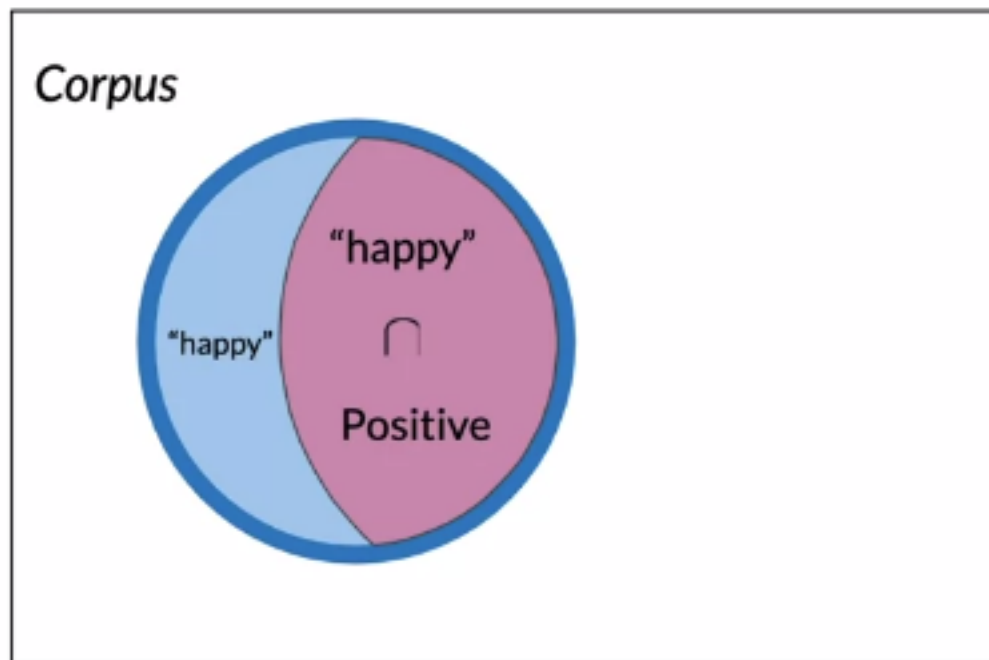


Conditional Probabilities



$$P(A | B) = P(\text{Positive} | \text{"happy"})$$

$$P(A | B) = 3 / 4 = 0.75$$

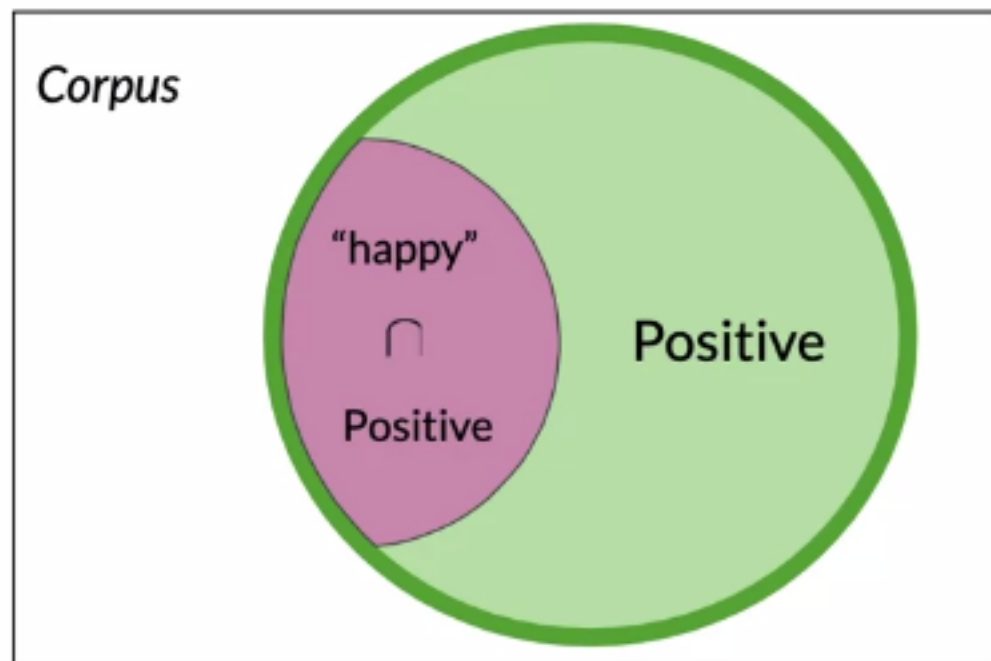


Conditional Probabilities

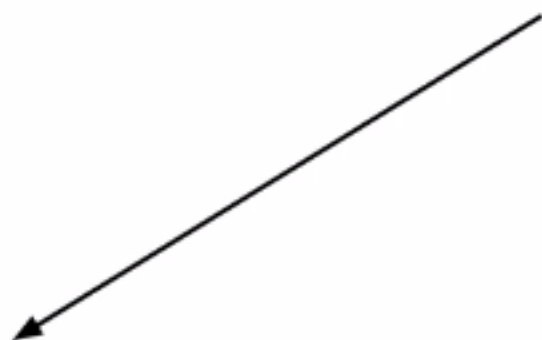


$$P(B | A) = P(\text{"happy"} | \text{Positive})$$

$$P(B | A) = 3 / 13 = 0.231$$

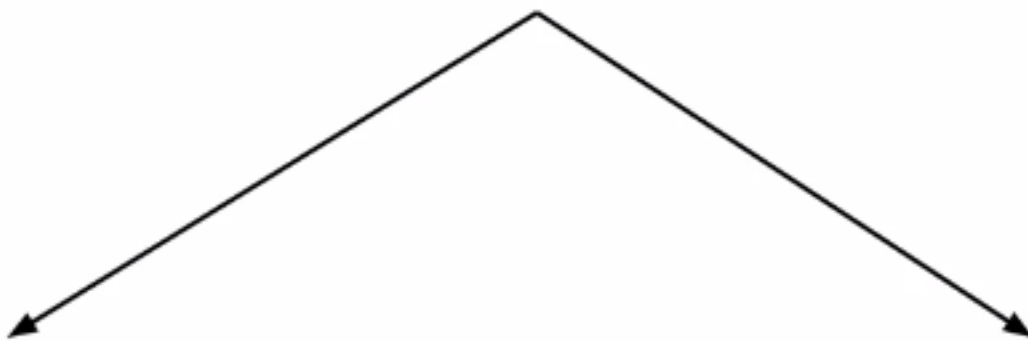


Conditional probabilities



Probability of B, given A happened

Conditional probabilities

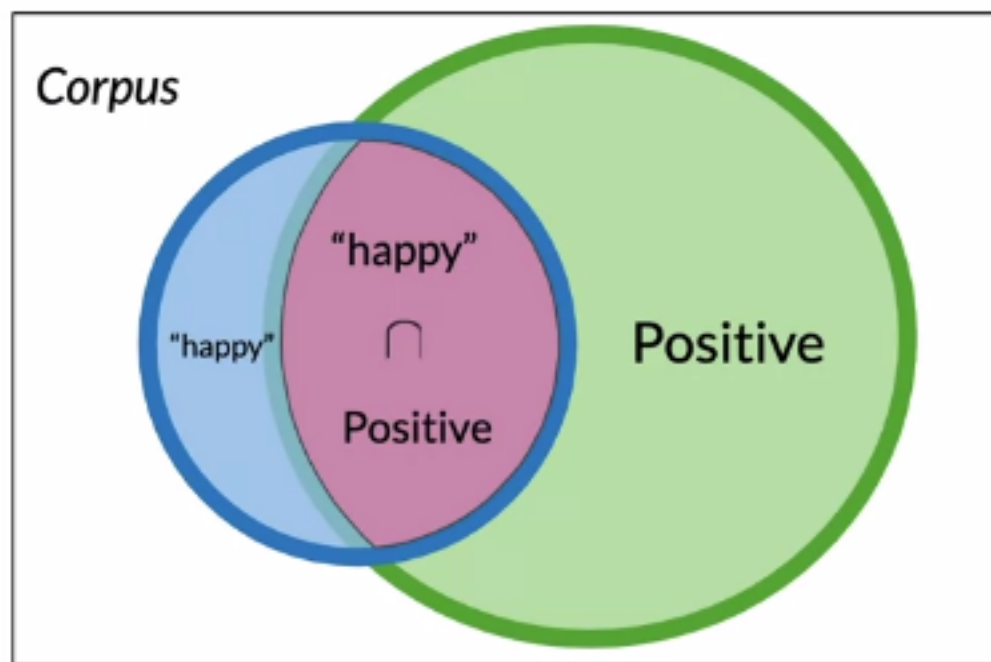


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graph TD; A[Conditional probabilities] --> B[Probability of B, given A happened]; A --> C[Looking at the elements of set A, the chance that one also belongs to set B]
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Probability of B, given A happened

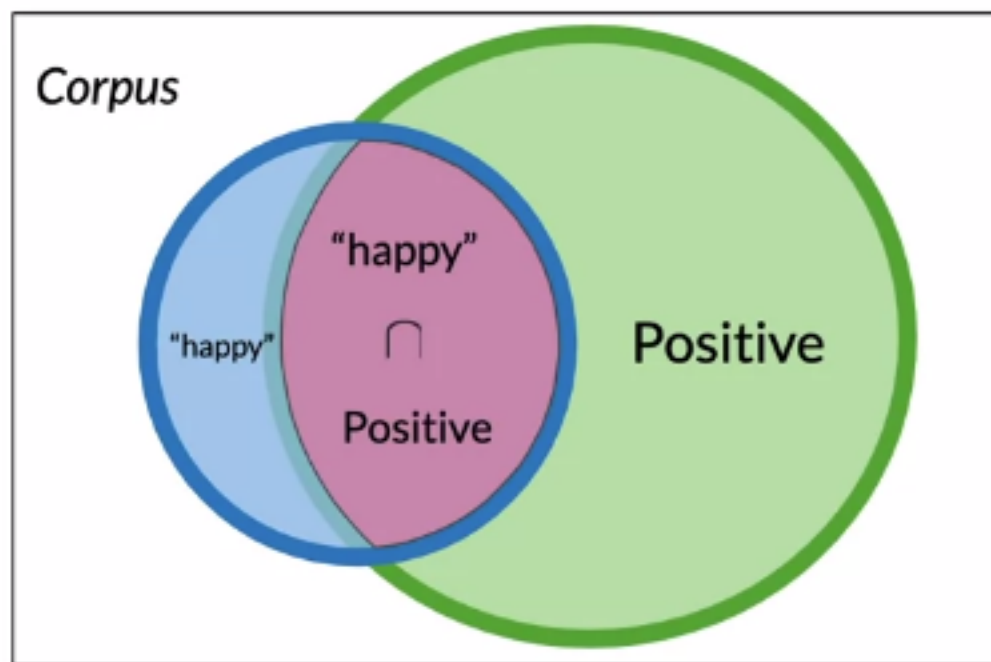
Looking at the elements of set A, the chance that one also belongs to set B

Conditional probabilities



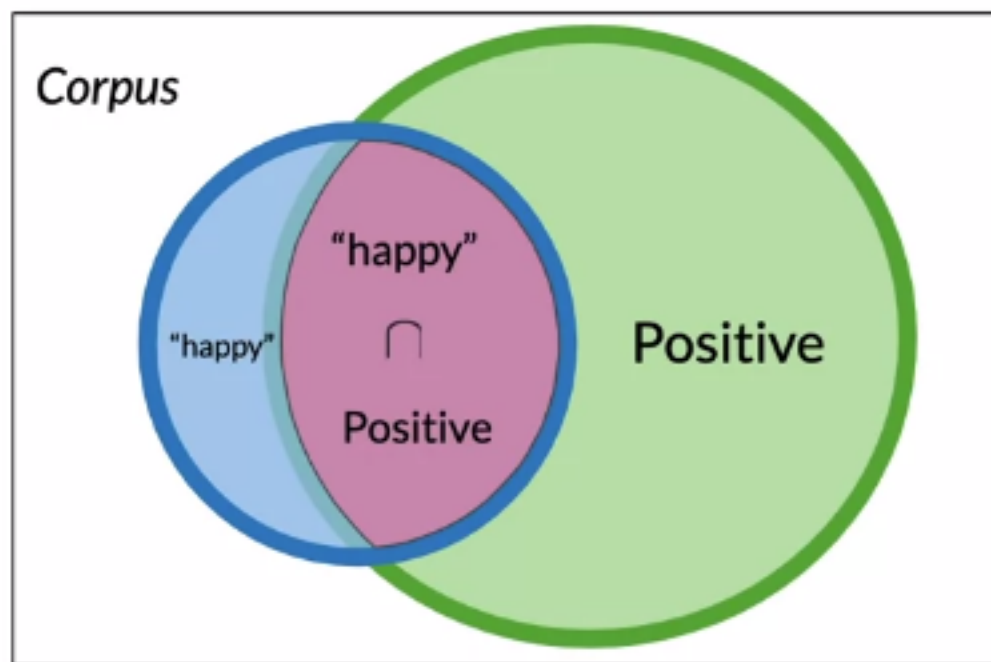
$$P(\text{Positive} | \text{"happy"}) =$$

Conditional probabilities



$$P(\text{Positive} | \text{"happy"}) = \frac{P(\text{Positive} \cap \text{"happy"})}{P(\text{"happy"})}$$

Conditional probabilities



$$P(\text{Positive} | \text{"happy"}) = \frac{P(\text{Positive} \cap \text{"happy"})}{P(\text{"happy"})}$$

Bayes' rule

$$P(\text{Positive} | \text{"happy"}) = \frac{P(\text{Positive} \cap \text{"happy"})}{P(\text{"happy"})}$$

Bayes' rule

$$P(\text{Positive} | \text{"happy"}) = \frac{P(\text{Positive} \cap \text{"happy"})}{P(\text{"happy"})}$$

$$P(\text{"happy"} | \text{Positive}) = \frac{P(\text{"happy"} \cap \text{Positive})}{P(\text{Positive})}$$

Bayes' rule

$$P(\text{Positive} | \text{"happy"}) = \frac{P(\text{Positive} \cap \text{"happy"})}{P(\text{"happy"})}$$

$$P(\text{"happy"} | \text{Positive}) = \frac{P(\text{"happy"} \cap \text{Positive})}{P(\text{Positive})}$$

Bayes' rule

$$P(\text{Positive} | \text{"happy"}) = P(\text{"happy"} | \text{Positive}) \times \frac{P(\text{Positive})}{P(\text{"happy"})}$$

Bayes' rule

$$P(\text{Positive} | \text{"happy"}) = P(\text{"happy"} | \text{Positive}) \times \frac{P(\text{Positive})}{P(\text{"happy"})}$$

$$P(X|Y)$$

Bayes' rule

$$P(\text{Positive} | \text{"happy"}) = P(\text{"happy"} | \text{Positive}) \times \frac{P(\text{Positive})}{P(\text{"happy"})}$$

$$P(X|Y) = P(Y|X)$$

Bayes' rule

$$P(\text{Positive} | \text{"happy"}) = P(\text{"happy"} | \text{Positive}) \times \frac{P(\text{Positive})}{P(\text{"happy"})}$$

$$P(X|Y) = P(Y|X) \times \frac{P(X)}{P(Y)}$$

Summary

- Conditional probabilities \longrightarrow Bayes' Rule
- $P(X|Y) = P(Y|X) \times \frac{P(X)}{P(Y)}$

Naïve Bayes for Sentiment Analysis

Positive tweets

I am happy because I am learning NLP

I am happy, not sad.

Negative tweets

I am sad, I am not learning NLP

I am sad, not happy

Naïve Bayes for Sentiment Analysis

Positive tweets

I am happy because I am learning NLP

I am happy, not sad.

Negative tweets

I am sad, I am not learning NLP

I am sad, not happy

word

I

am

happy

because

learning

NLP

sad

not

Naïve Bayes for Sentiment Analysis

Positive tweets

I am happy because I am learning NLP

I am happy, not sad.

Negative tweets

I am sad, I am not learning NLP

I am sad, not happy

| word | Pos |
|----------|-----|
| I | 3 |
| am | 3 |
| happy | 2 |
| because | 1 |
| learning | 1 |
| NLP | 1 |
| sad | 1 |
| not | 1 |

Naïve Bayes for Sentiment Analysis

Positive tweets

I am happy because I am learning NLP

I am happy, not sad.

Negative tweets

I am sad, I am not learning NLP

I am sad, not happy

| word | Pos | Neg |
|----------|-----|-----|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |

Naïve Bayes for Sentiment Analysis

Positive tweets

I am happy because I am learning NLP

I am happy, not sad.

Negative tweets

I am sad, I am not learning NLP

I am sad, not happy

| word | Pos | Neg |
|--------------------|-----|-----|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| N_{class} | 13 | 12 |

$P(w_i | \text{class})$

| word | Pos | Neg |
|----------|-----|-----|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

$$p(I|Pos) = \frac{3}{13}$$

| word | Pos | Neg |
|------|------|-----|
| I | 0.24 | - |

$P(w_i | \text{class})$

| word | Pos | Neg |
|----------|-----|-----|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

$$p(I|Pos) = \frac{3}{13}$$

| word | Pos | Neg |
|------|------|-----|
| I | 0.24 | - |

$P(w_i | \text{class})$

| word | Pos | Neg |
|---------------|-----------|-----------|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

$$p(I|Neg) = \frac{3}{12}$$

| word | Pos | Neg |
|------|------|------|
| I | 0.24 | 0.25 |

$$P(w_i | \text{class})$$

| word | Pos | Neg |
|---------------|-----------|-----------|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

| word | Pos | Neg |
|----------|------|------|
| I | 0.24 | 0.25 |
| am | 0.24 | 0.25 |
| happy | 0.15 | 0.08 |
| because | 0.08 | 0.00 |
| learning | 0.08 | 0.08 |
| NLP | 0.08 | 0.08 |
| sad | 0.08 | 0.17 |
| not | 0.08 | 0.17 |

$$P(w_i | \text{class})$$

| word | Pos | Neg |
|---------------|-----------|-----------|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

| word | Pos | Neg |
|------------|----------|----------|
| I | 0.24 | 0.25 |
| am | 0.24 | 0.25 |
| happy | 0.15 | 0.08 |
| because | 0.08 | 0.00 |
| learning | 0.08 | 0.08 |
| NLP | 0.08 | 0.08 |
| sad | 0.08 | 0.17 |
| not | 0.08 | 0.17 |
| Sum | 1 | 1 |

$P(w_i | \text{class})$

| word | Pos | Neg |
|----------|------|------|
| I | 0.24 | 0.25 |
| am | 0.24 | 0.25 |
| happy | 0.15 | 0.08 |
| because | 0.08 | 0 |
| learning | 0.08 | 0.08 |
| NLP | 0.08 | 0.08 |
| sad | 0.08 | 0.17 |
| not | 0.08 | 0.17 |

Naïve Bayes

Tweet: I am happy today; I am learning.

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

$$\frac{0.20}{0.20}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10} * \frac{0.20}{0.20}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10} * \frac{0.20}{0.20} * \frac{0.20}{0.20}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10} * \frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.10}{0.10}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10} * \frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.10}{0.10}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)} = \frac{0.14}{0.10} = 1.4$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10} * \frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.10}{0.10}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Naïve Bayes

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)} = \frac{0.14}{0.10} = 1.4 > 1$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10} * \frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.10}{0.10}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Summary

- Naive Bayes inference condition rule for binary classification
- Table of probabilities

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

Laplacian Smoothing

$$P(w_i | \text{class}) = \frac{\text{freq}(w_i, \text{class})}{N_{\text{class}}}$$

class \in {Positive, Negative}

N_{class} = frequency of all words in class

V = number of unique words in vocabulary

Laplacian Smoothing

$$P(w_i | \text{class}) = \frac{\text{freq}(w_i, \text{class})}{N_{\text{class}}} \quad \text{class} \in \{\text{Positive}, \text{Negative}\}$$

$$P(w_i | \text{class}) = \frac{\text{freq}(w_i, \text{class}) + 1}{N_{\text{class}} + V}$$

N_{class} = frequency of all words in class

V = number of unique words in vocabulary

Introducing $P(w_i | \text{class})$ with smoothing

| word | Pos | Neg |
|---------------|-----------|-----------|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

| word | Pos | Neg |
|------|-----|-----|
|------|-----|-----|

Introducing $P(w_i | \text{class})$ with smoothing

| word | Pos | Neg |
|---------------|-----------|-----------|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

| word | Pos | Neg |
|------|-----|-----|
| I | - | - |

$$V = 8$$

Introducing $P(w_i | \text{class})$ with smoothing

| word | Pos | Neg |
|----------|-----|-----|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

$$P(I|Pos) = \frac{3 + 1}{13 + 8}$$

$$V = 8$$

| word | Pos | Neg |
|------|-----|-----|
| I | - | - |

Introducing $P(w_i | \text{class})$ with smoothing

| word | Pos | Neg |
|----------|-----|-----|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

$$P(I|Pos) = \frac{3 + 1}{13 + 8}$$

$$V = 8$$

| word | Pos | Neg |
|------|------|-----|
| I | 0.19 | - |

Introducing $P(w_i | \text{class})$ with smoothing

| word | Pos | Neg |
|---------------|-----------|-----------|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

$$P(I|Neg) = \frac{3 + 1}{12 + 8}$$

$$V = 8$$

| word | Pos | Neg |
|------|------|-----|
| I | 0.19 | - |

Introducing $P(w_i | \text{class})$ with smoothing

| word | Pos | Neg |
|---------------|-----------|-----------|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

$$P(I|Neg) = \frac{3 + 1}{12 + 8}$$

$$V = 8$$

| word | Pos | Neg |
|------|------|------|
| I | 0.19 | 0.20 |

Introducing $P(w_i | \text{class})$ with smoothing

| word | Pos | Neg |
|---------------|-----------|-----------|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

$$V = 8$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.19 | 0.20 |
| am | 0.19 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

Introducing $P(w_i | \text{class})$ with smoothing

| word | Pos | Neg |
|---------------|-----------|-----------|
| I | 3 | 3 |
| am | 3 | 3 |
| happy | 2 | 1 |
| because | 1 | 0 |
| learning | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| Nclass | 13 | 12 |

$$V = 8$$

| word | Pos | Neg |
|------------|----------|----------|
| I | 0.19 | 0.20 |
| am | 0.19 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |
| Sum | 1 | 1 |

Summary

- Laplacian smoothing to avoid $P(w_i|class) = 0$
- Naïve Bayes formula

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

Ratio of probabilities

| word | Pos | Neg |
|----------|------|------|
| I | 0.20 | 0.20 |
| am | 0.20 | 0.20 |
| happy | 0.14 | 0.10 |
| because | 0.10 | 0.10 |
| learning | 0.10 | 0.10 |
| NLP | 0.10 | 0.10 |
| sad | 0.10 | 0.15 |
| not | 0.10 | 0.15 |

$$\text{ratio}(w_i) = \frac{P(w_i | \text{Pos})}{P(w_i | \text{Neg})}$$

Ratio of probabilities

| word | Pos | Neg | ratio |
|----------|------|------|-------|
| I | 0.20 | 0.20 | |
| am | 0.20 | 0.20 | |
| happy | 0.14 | 0.10 | |
| because | 0.10 | 0.10 | |
| learning | 0.10 | 0.10 | |
| NLP | 0.10 | 0.10 | |
| sad | 0.10 | 0.15 | |
| not | 0.10 | 0.15 | |

$$\text{ratio}(w_i) = \frac{P(w_i | \text{Pos})}{P(w_i | \text{Neg})}$$

Ratio of probabilities

| word | Pos | Neg | ratio |
|----------|------|------|-------|
| I | 0.20 | 0.20 | 1 |
| am | 0.20 | 0.20 | 1 |
| happy | 0.14 | 0.10 | 1.4 |
| because | 0.10 | 0.10 | 1 |
| learning | 0.10 | 0.10 | 1 |
| NLP | 0.10 | 0.10 | 1 |
| sad | 0.10 | 0.15 | 0.6 |
| not | 0.10 | 0.15 | 0.6 |

$$\text{ratio}(w_i) = \frac{P(w_i | \text{Pos})}{P(w_i | \text{Neg})}$$

Ratio of probabilities

Positive ∞

Neutral 1

Negative 0

| word | Pos | Neg | ratio |
|----------|------|------|-------|
| I | 0.20 | 0.20 | 1 |
| am | 0.20 | 0.20 | 1 |
| happy | 0.14 | 0.10 | 1.4 |
| because | 0.10 | 0.10 | 1 |
| learning | 0.10 | 0.10 | 1 |
| NLP | 0.10 | 0.10 | 1 |
| sad | 0.10 | 0.15 | 0.6 |
| not | 0.10 | 0.15 | 0.6 |

$$\text{ratio}(w_i) = \frac{P(w_i | \text{Pos})}{P(w_i | \text{Neg})}$$

Ratio of probabilities

Positive \uparrow ∞

Neutral 1

Negative \downarrow 0

| word | Pos | Neg | ratio |
|----------|------|------|-------|
| I | 0.20 | 0.20 | 1 |
| am | 0.20 | 0.20 | 1 |
| happy | 0.14 | 0.10 | 1.4 |
| because | 0.10 | 0.10 | 1 |
| learning | 0.10 | 0.10 | 1 |
| NLP | 0.10 | 0.10 | 1 |
| sad | 0.10 | 0.15 | 0.6 |
| not | 0.10 | 0.15 | 0.6 |

$$\text{ratio}(w_i) = \frac{P(w_i | \text{Pos})}{P(w_i | \text{Neg})}$$

$$\approx \frac{\text{freq}(w_i, 1) + 1}{\text{freq}(w_i, 0) + 1}$$

Naïve Bayes' inference

$class \in \{pos, neg\}$

$w \rightarrow$ Set of m words in a tweet

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)} > 1$$

Naïve Bayes' inference

$class \in \{pos, neg\}$

$w \rightarrow$ Set of m words in a tweet

$$\frac{P(pos)}{P(neg)} \prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)} > 1$$

Naïve Bayes' inference

$class \in \{pos, neg\}$

$w \rightarrow$ Set of m words in a tweet

$$\frac{P(pos)}{P(neg)} \prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)} > 1$$

- A simple, fast, and powerful baseline
- A probabilistic model used for classification

Log Likelihood

- Products bring risk of underflow

Log Likelihood

$$\frac{P(pos)}{P(neg)} \prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

- Products bring risk of underflow
- $\log(a * b) = \log(a) + \log(b)$

Log Likelihood

$$\frac{P(pos)}{P(neg)} \prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

- Products bring risk of underflow
- $\log(a * b) = \log(a) + \log(b)$
- $\log\left(\frac{P(pos)}{P(neg)} \prod_{i=1}^n \frac{P(w_i|pos)}{P(w_i|neg)}\right)$

Log Likelihood

$$\frac{P(pos)}{P(neg)} \prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

- Products bring risk of underflow
- $\log(a * b) = \log(a) + \log(b)$

$$\bullet \log\left(\frac{P(pos)}{P(neg)} \prod_{i=1}^n \frac{P(w_i|pos)}{P(w_i|neg)}\right) \Rightarrow \log\frac{P(pos)}{P(neg)} + \sum_{i=1}^n \log\frac{P(w_i|pos)}{P(w_i|neg)}$$

log prior + log likelihood

Log Likelihood

$$\frac{P(pos)}{P(neg)} \prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$$

- Products bring risk of underflow
- $\log(a * b) = \log(a) + \log(b)$

$$\bullet \log\left(\frac{P(pos)}{P(neg)} \prod_{i=1}^n \frac{P(w_i|pos)}{P(w_i|neg)}\right) \Rightarrow \log\frac{P(pos)}{P(neg)} + \sum_{i=1}^n \log\frac{P(w_i|pos)}{P(w_i|neg)}$$

log prior + log likelihood

Calculating Lambda

tweet: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

| word | Pos | Neg |
|----------|------|------|
| I | 0.05 | 0.05 |
| am | 0.04 | 0.04 |
| happy | 0.09 | 0.01 |
| because | 0.01 | 0.01 |
| learning | 0.03 | 0.01 |
| NLP | 0.02 | 0.02 |
| sad | 0.01 | 0.09 |
| not | 0.02 | 0.03 |

Calculating Lambda

tweet: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(I) = \log \frac{0.05}{0.05}$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | |
| am | 0.04 | 0.04 | |
| happy | 0.09 | 0.01 | |
| because | 0.01 | 0.01 | |
| learning | 0.03 | 0.01 | |
| NLP | 0.02 | 0.02 | |
| sad | 0.01 | 0.09 | |
| not | 0.02 | 0.03 | |

Calculating Lambda

tweet: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(I) = \log \frac{0.05}{0.05} = \log(1) = 0$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | |
| am | 0.04 | 0.04 | |
| happy | 0.09 | 0.01 | |
| because | 0.01 | 0.01 | |
| learning | 0.03 | 0.01 | |
| NLP | 0.02 | 0.02 | |
| sad | 0.01 | 0.09 | |
| not | 0.02 | 0.03 | |

Calculating Lambda

tweet: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(I) = \log \frac{0.05}{0.05} = \log(1) = 0$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | |
| happy | 0.09 | 0.01 | |
| because | 0.01 | 0.01 | |
| learning | 0.03 | 0.01 | |
| NLP | 0.02 | 0.02 | |
| sad | 0.01 | 0.09 | |
| not | 0.02 | 0.03 | |

Calculating Lambda

tweet: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(am) = \log \frac{0.04}{0.04}$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | |
| happy | 0.09 | 0.01 | |
| because | 0.01 | 0.01 | |
| learning | 0.03 | 0.01 | |
| NLP | 0.02 | 0.02 | |
| sad | 0.01 | 0.09 | |
| not | 0.02 | 0.03 | |

Calculating Lambda

tweet: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(am) = \log \frac{0.04}{0.04} = \log(1) = 0$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | |
| happy | 0.09 | 0.01 | |
| because | 0.01 | 0.01 | |
| learning | 0.03 | 0.01 | |
| NLP | 0.02 | 0.02 | |
| sad | 0.01 | 0.09 | |
| not | 0.02 | 0.03 | |

Calculating Lambda

tweet: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(am) = \log \frac{0.04}{0.04} = \log(1) = 0$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | |
| because | 0.01 | 0.01 | |
| learning | 0.03 | 0.01 | |
| NLP | 0.02 | 0.02 | |
| sad | 0.01 | 0.09 | |
| not | 0.02 | 0.03 | |

Summing the Lambdas

doc: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(\text{happy}) = \log \frac{0.09}{0.01} \approx 2.2$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | |
| because | 0.01 | 0.01 | |
| learning | 0.03 | 0.01 | |
| NLP | 0.02 | 0.02 | |
| sad | 0.01 | 0.09 | |
| not | 0.02 | 0.03 | |

Summing the Lambdas

doc: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(\text{happy}) = \log \frac{0.09}{0.01} \approx 2.2$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | 2.2 |
| because | 0.01 | 0.01 | |
| learning | 0.03 | 0.01 | |
| NLP | 0.02 | 0.02 | |
| sad | 0.01 | 0.09 | |
| not | 0.02 | 0.03 | |

Summing the Lambdas

doc: I am happy because I am learning.

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(\text{happy}) = \log \frac{0.09}{0.01} \approx 2.2$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | 2.2 |
| because | 0.01 | 0.01 | 0 |
| learning | 0.03 | 0.01 | 1.1 |
| NLP | 0.02 | 0.02 | 0 |
| sad | 0.01 | 0.09 | -2.2 |
| not | 0.02 | 0.03 | -0.4 |

Summary

- Word sentiment

$$ratio(w) = \frac{P(w|pos)}{P(w|neg)}$$

$$\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$$



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Log Likelihood, Part 2

Log Likelihood

doc: I am happy because I am learning.

$$\sum_{i=1}^m \log \frac{P(w_i|pos)}{P(w_i|neg)} = \sum_{i=1}^m \lambda(w_i)$$

log likelihood =

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | 2.2 |
| because | 0.01 | 0.01 | 0 |
| learning | 0.03 | 0.01 | 1.1 |
| NLP | 0.02 | 0.02 | 0 |
| sad | 0.01 | 0.09 | -2.2 |
| not | 0.02 | 0.03 | -0.4 |

Log Likelihood

doc: I am happy because I am learning.

$$\sum_{i=1}^m \log \frac{P(w_i|pos)}{P(w_i|neg)} = \sum_{i=1}^m \lambda(w_i)$$

log likelihood = 0

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | 2.2 |
| because | 0.01 | 0.01 | 0 |
| learning | 0.03 | 0.01 | 1.1 |
| NLP | 0.02 | 0.02 | 0 |
| sad | 0.01 | 0.09 | -2.2 |
| not | 0.02 | 0.03 | -0.4 |

Log Likelihood

doc: I am happy because I am learning.

$$\sum_{i=1}^m \log \frac{P(w_i|pos)}{P(w_i|neg)} = \sum_{i=1}^m \lambda(w_i)$$

log likelihood = 0 + 0

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | 2.2 |
| because | 0.01 | 0.01 | 0 |
| learning | 0.03 | 0.01 | 1.1 |
| NLP | 0.02 | 0.02 | 0 |
| sad | 0.01 | 0.09 | -2.2 |
| not | 0.02 | 0.03 | -0.4 |

Log Likelihood

doc: I am happy because I am learning.

$$\sum_{i=1}^m \log \frac{P(w_i|pos)}{P(w_i|neg)} = \sum_{i=1}^m \lambda(w_i)$$

log likelihood = 0 + 0 + 2.2

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | 2.2 |
| because | 0.01 | 0.01 | 0 |
| learning | 0.03 | 0.01 | 1.1 |
| NLP | 0.02 | 0.02 | 0 |
| sad | 0.01 | 0.09 | -2.2 |
| not | 0.02 | 0.03 | -0.4 |

Log Likelihood

doc: I am happy because I am learning.

$$\sum_{i=1}^m \log \frac{P(w_i|pos)}{P(w_i|neg)} = \sum_{i=1}^m \lambda(w_i)$$

log likelihood = 0 + 0 + 2.2 + 0 + 0 + 0

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | 2.2 |
| because | 0.01 | 0.01 | 0 |
| learning | 0.03 | 0.01 | 1.1 |
| NLP | 0.02 | 0.02 | 0 |
| sad | 0.01 | 0.09 | -2.2 |
| not | 0.02 | 0.03 | -0.4 |

Log Likelihood

doc: I am happy because I am learning.

$$\sum_{i=1}^m \log \frac{P(w_i|pos)}{P(w_i|neg)} = \sum_{i=1}^m \lambda(w_i)$$

log likelihood = 0 + 0 + 2.2 + 0 + 0 + 0 + 1.1

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | 2.2 |
| because | 0.01 | 0.01 | 0 |
| learning | 0.03 | 0.01 | 1.1 |
| NLP | 0.02 | 0.02 | 0 |
| sad | 0.01 | 0.09 | -2.2 |
| not | 0.02 | 0.03 | -0.4 |

Log Likelihood

doc: I am happy because I am learning.

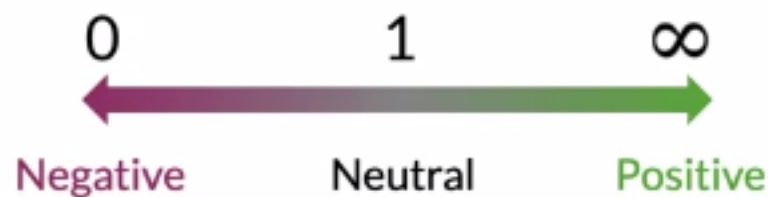
$$\sum_{i=1}^m \log \frac{P(w_i|pos)}{P(w_i|neg)} = \sum_{i=1}^m \lambda(w_i)$$

$$\text{log likelihood} = 0 + 0 + 2.2 + 0 + 0 + 0 + 1.1 = 3.3$$

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| I | 0.05 | 0.05 | 0 |
| am | 0.04 | 0.04 | 0 |
| happy | 0.09 | 0.01 | 2.2 |
| because | 0.01 | 0.01 | 0 |
| learning | 0.03 | 0.01 | 1.1 |
| NLP | 0.02 | 0.02 | 0 |
| sad | 0.01 | 0.09 | -2.2 |
| not | 0.02 | 0.03 | -0.4 |

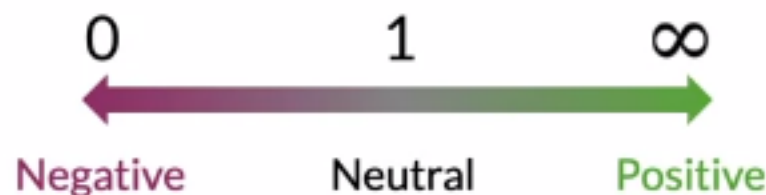
Log Likelihood

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)} > 1$$

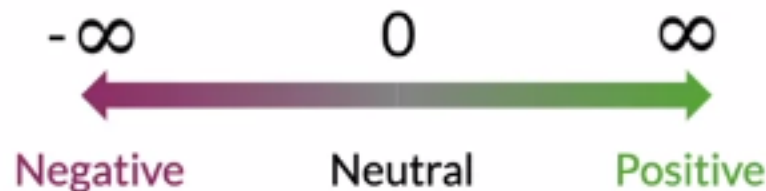


Log Likelihood

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)} > 1$$

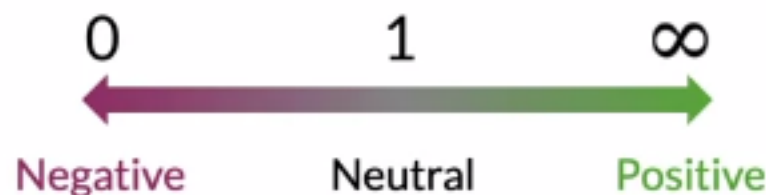


$$\sum_{i=1}^m \log \frac{P(w_i|pos)}{P(w_i|neg)} > 0$$

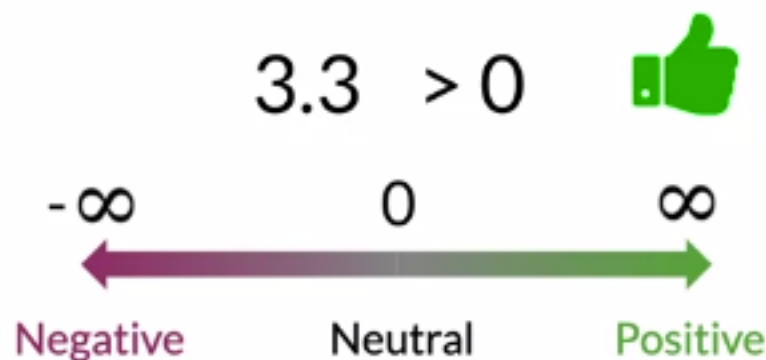


Log Likelihood

$$\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)} > 1$$



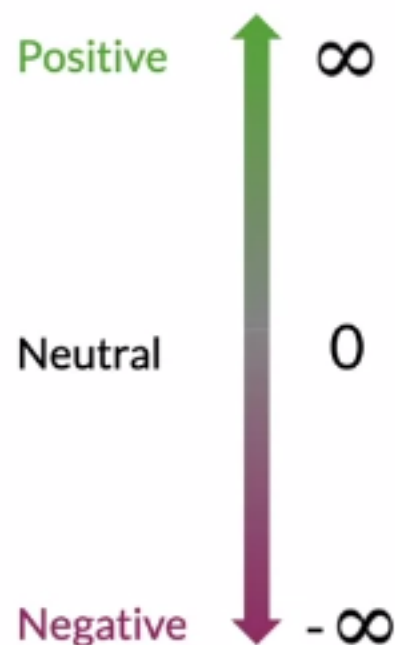
$$\sum_{i=1}^m \log \frac{P(w_i|pos)}{P(w_i|neg)} > 0$$



Summary

Tweet sentiment:

$$\log \prod_{i=1}^m \text{ratio}(w_i) = \sum_{i=1}^m \lambda(w_i) > 0$$



Outline

- Five steps for training a Naïve Bayes model

Training Naïve Bayes

Step 0: Collect and annotate corpus

Training Naïve Bayes

Step 0: Collect and annotate corpus

Positive tweets

I am happy because I am learning NLP
I am happy, not sad. @NLP

Negative tweets

I am sad, I am not learning NLP
I am sad, not happy!!

Training Naïve Bayes

Step 0: Collect and annotate corpus

Positive tweets

I am happy because I am learning NLP
I am happy, not sad. @NLP

Negative tweets

I am sad, I am not learning NLP
I am sad, not happy!!

Step 1:
Preprocess

- Lowercase
- Remove punctuation, urls, names
- Remove stop words
- Stemming
- Tokenize sentences

Training Naïve Bayes

Step 0: Collect and annotate corpus

Positive tweets

I am happy because I am learning NLP
I am happy, not sad. @NLP

Negative tweets

I am sad, I am not learning NLP
I am sad, not happy!!

Step 1:
Preprocess

- Lowercase
- Remove punctuation, urls, names
- Remove stop words
- Stemming
- Tokenize sentences

Positive tweets

[happi, because, learn, NLP]
[happi, not, sad]

Negative tweets

[sad, not, learn, NLP]
[sad, not, happi]

Training Naïve Bayes

Positive tweets

[happi, because, learn, NLP]

[happi, not, sad]

Negative tweets

[sad, not, learn, NLP]

[sad, not, happi]

Training Naïve Bayes

$\text{freq}(w, \text{class})$

Positive tweets

[happi, because, learn, NLP]

[happi, not, sad]

Negative tweets

[sad, not, learn, NLP]

[sad, not, happi]

Step 2:
Word
count

Training Naïve Bayes

Positive tweets

[happi, because, learn, NLP]

[happi, not, sad]

Negative tweets

[sad, not, learn, NLP]

[sad, not, happi]

Step 2:
Word
count

freq(w, class)

| word | Pos | Neg |
|--------------------|-----|-----|
| happi | 2 | 1 |
| because | 1 | 0 |
| learn | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| N_{class} | 7 | 7 |

Training Naïve Bayes

| freq(w, class) | | |
|--------------------|-----|-----|
| word | Pos | Neg |
| happi | 2 | 1 |
| because | 1 | 0 |
| learn | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| N_{class} | 7 | 7 |

Training Naïve Bayes

| freq(w, class) | | |
|--------------------|-----|-----|
| word | Pos | Neg |
| happi | 2 | 1 |
| because | 1 | 0 |
| learn | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| N_{class} | 7 | 7 |

Step 3:
 $P(w|\text{class})$

$$V_{\text{class}} = 6$$

$$\frac{\text{freq}(w, \text{class}) + 1}{N_{\text{class}} + V_{\text{class}}}$$

Training Naïve Bayes

freq(w, class)

| word | Pos | Neg |
|--------------------|-----|-----|
| happi | 2 | 1 |
| because | 1 | 0 |
| learn | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| N_{class} | 7 | 7 |

Step 3:
 $P(w|\text{class})$

$$V_{\text{class}} = 6$$

$$\frac{\text{freq}(w, \text{class}) + 1}{N_{\text{class}} + V_{\text{class}}}$$

| word | Pos | Neg |
|----------|------|------|
| happy | 0.23 | 0.15 |
| because | 0.15 | 0.07 |
| learning | 0.08 | 0.08 |
| NLP | 0.08 | 0.08 |
| sad | 0.08 | 0.17 |
| not | 0.08 | 0.17 |

Training Naïve Bayes

| freq(w, class) | | |
|--------------------|-----|-----|
| word | Pos | Neg |
| happi | 2 | 1 |
| because | 1 | 0 |
| learn | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| N_{class} | 7 | 7 |

Step 3:
 $P(w|\text{class})$

$$V_{\text{class}} = 6$$

$$\frac{\text{freq}(w, \text{class}) + 1}{N_{\text{class}} + V_{\text{class}}}$$

$$\lambda(w) = \log \frac{P(w|\text{pos})}{P(w|\text{neg})}$$

Step 4: Get
lambda

| word | Pos | Neg |
|----------|------|------|
| happy | 0.23 | 0.15 |
| because | 0.15 | 0.07 |
| learning | 0.08 | 0.08 |
| NLP | 0.08 | 0.08 |
| sad | 0.08 | 0.17 |
| not | 0.08 | 0.17 |

Training Naïve Bayes

| freq(w, class) | | |
|--------------------|-----|-----|
| word | Pos | Neg |
| happi | 2 | 1 |
| because | 1 | 0 |
| learn | 1 | 1 |
| NLP | 1 | 1 |
| sad | 1 | 2 |
| not | 1 | 2 |
| N_{class} | 7 | 7 |

Step 3:
 $P(w|\text{class})$

$$V_{\text{class}} = 6$$

$$\frac{\text{freq}(w, \text{class}) + 1}{N_{\text{class}} + V_{\text{class}}}$$

$$\lambda(w) = \log \frac{P(w|\text{pos})}{P(w|\text{neg})}$$

Step 4: Get
lambda

| word | Pos | Neg | λ |
|----------|------|------|-----------|
| happy | 0.23 | 0.15 | 0.43 |
| because | 0.15 | 0.07 | 0.6 |
| learning | 0.08 | 0.08 | 0 |
| NLP | 0.08 | 0.08 | 0 |
| sad | 0.08 | 0.17 | -0.75 |
| not | 0.08 | 0.17 | -0.75 |

Training Naïve Bayes

Step 5:
Get the
log prior

D_{pos} = Number of positive tweets
 D_{neg} = Number of negative tweets

$$\text{logprior} = \log \frac{D_{pos}}{D_{neg}}$$

Training Naïve Bayes

Step 5:
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Training Naïve Bayes

Step 5:
Get the
log prior

D_{pos} = Number of positive tweets
 D_{neg} = Number of negative tweets

$$\text{logprior} = \log \frac{D_{pos}}{D_{neg}}$$

If dataset is balanced, $D_{pos} = D_{neg}$ and $\text{logprior} = 0$.

Summary

0. Get or annotate a dataset with positive and negative tweets
1. Preprocess the tweets: $\text{process_tweet}(\text{tweet}) \rightarrow [w_1, w_2, w_3, \dots]$
2. Compute $\text{freq}(w, \text{class})$
3. Get $P(w \mid \text{pos}), P(w \mid \text{neg})$
4. Get $\lambda(w)$
5. Compute $\text{logprior} = \log(P(\text{pos}) / P(\text{neg}))$

Outline

- Predict using a Näive Bayes Model
- Using your validation set to compute model accuracy

Predict using Naïve Bayes

- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$

| word | λ |
|---------|-----------|
| I | -0.01 |
| the | -0.01 |
| happi | 0.63 |
| because | 0.01 |
| pass | 0.5 |
| NLP | 0 |
| sad | -0.75 |
| not | -0.75 |

Predict using Naïve Bayes

- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$
- $logprior = \log \frac{D_{pos}}{D_{neg}} = 0$

| word | λ |
|---------|-----------|
| I | -0.01 |
| the | -0.01 |
| happi | 0.63 |
| because | 0.01 |
| pass | 0.5 |
| NLP | 0 |
| sad | -0.75 |
| not | -0.75 |

Predict using Naïve Bayes

- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$
- $logprior = \log \frac{D_{pos}}{D_{neg}} = 0$
- Tweet: I passed the NLP interview.

| word | λ |
|---------|-----------|
| I | -0.01 |
| the | -0.01 |
| happi | 0.63 |
| because | 0.01 |
| pass | 0.5 |
| NLP | 0 |
| sad | -0.75 |
| not | -0.75 |

Predict using Naïve Bayes

- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$
- $logprior = \log \frac{D_{pos}}{D_{neg}} = 0$
- Tweet: [I, pass, the, NLP, interview]

| word | λ |
|---------|-----------|
| I | -0.01 |
| the | -0.01 |
| happi | 0.63 |
| because | 0.01 |
| pass | 0.5 |
| NLP | 0 |
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Predict using Naïve Bayes

- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$
- $logprior = \log \frac{D_{pos}}{D_{neg}} = 0$
- Tweet: [I, pass, the, NLP, interview]

| word | λ |
|---------|-----------|
| I | -0.01 |
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| NLP | 0 |
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| not | -0.75 |

Predict using Naïve Bayes

- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$
- $logprior = \log \frac{D_{pos}}{D_{neg}} = 0$
- Tweet: [I, pass, the, NLP, interview]

$$score = -0.01 + 0.5 - 0.01 + 0$$

| word | λ |
|---------|-----------|
| I | -0.01 |
| the | -0.01 |
| happi | 0.63 |
| because | 0.01 |
| pass | 0.5 |
| NLP | 0 |
| sad | -0.75 |
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Predict using Naïve Bayes

- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$
- $logprior = \log \frac{D_{pos}}{D_{neg}} = 0$
- Tweet: [I, pass, the, NLP, interview]

$$score = -0.01 + 0.5 - 0.01 + 0 + logprior$$

| word | λ |
|---------|-----------|
| I | -0.01 |
| the | -0.01 |
| happi | 0.63 |
| because | 0.01 |
| pass | 0.5 |
| NLP | 0 |
| sad | -0.75 |
| not | -0.75 |

Predict using Naïve Bayes

- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$
- $logprior = \log \frac{D_{pos}}{D_{neg}} = 0$
- Tweet: [I, pass, the, NLP, interview]

$$score = -0.01 + 0.5 - 0.01 + 0 + logprior = 0.48$$

| word | λ |
|---------|-----------|
| I | -0.01 |
| the | -0.01 |
| happi | 0.63 |
| because | 0.01 |
| pass | 0.5 |
| NLP | 0 |
| sad | -0.75 |
| not | -0.75 |

Predict using Naïve Bayes


- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$
- $logprior = \log \frac{D_{pos}}{D_{neg}} = 0$
- Tweet: [I, pass, the, NLP, interview]

$$score = -0.01 + 0.5 - 0.01 + 0 + logprior = 0.48$$

$$pred = score > 0$$

| word | λ |
|---------|-----------|
| I | -0.01 |
| the | -0.01 |
| happi | 0.63 |
| because | 0.01 |
| pass | 0.5 |
| NLP | 0 |
| sad | -0.75 |
| not | -0.75 |

Predict using Naïve Bayes

- log-likelihood dictionary $\lambda(w) = \log \frac{P(w|pos)}{P(w|neg)}$
- $logprior = \log \frac{D_{pos}}{D_{neg}} = 0$
- Tweet: [I, pass, the, NLP, interview] 

$$score = -0.01 + 0.5 - 0.01 + 0 + logprior = 0.48$$

$$pred = score > 0$$

| word | λ |
|---------|-----------|
| I | -0.01 |
| the | -0.01 |
| happi | 0.63 |
| because | 0.01 |
| pass | 0.5 |
| NLP | 0 |
| sad | -0.75 |
| not | -0.75 |

Testing Naïve Bayes

- $X_{val} \ Y_{val}$

Testing Naïve Bayes

- $X_{val} \ Y_{val} \ \lambda \ \logprior$

Testing Naïve Bayes

- X_{val} Y_{val} λ $logprior$

$score = predict(X_{val}, \lambda, logprior)$

$$\begin{bmatrix} 0.5 \\ -1 \\ 1.3 \\ \vdots \\ score_m \end{bmatrix}$$

Testing Naïve Bayes

- X_{val} Y_{val} λ \logprior

$$score = predict(X_{val}, \lambda, \logprior)$$

$$pred = score > 0 \quad \begin{bmatrix} 0.5 \\ -1 \\ 1.3 \\ \vdots \\ score_m \end{bmatrix} > 0 = \begin{bmatrix} 0.5 > 0 \\ -1 > 0 \\ 1.3 > 0 \\ \vdots \\ score_m > 0 \end{bmatrix}$$

Testing Naïve Bayes

- X_{val} Y_{val} λ $logprior$

$$score = predict(X_{val}, \lambda, logprior)$$

$$pred = score > 0 \quad \begin{bmatrix} 0.5 \\ -1 \\ 1.3 \\ \vdots \\ score_m \end{bmatrix} > 0 = \begin{bmatrix} 0.5 > 0 \\ -1 > 0 \\ 1.3 > 0 \\ \vdots \\ score_m > 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 1 \\ \vdots \\ pred_m \end{bmatrix}$$

Testing Naïve Bayes

- X_{val} Y_{val} λ \logprior

$score = predict(X_{val}, \lambda, \logprior)$

$pred = score > 0$

$$\frac{1}{m} \sum_{i=1}^m (pred_i == Y_{val_i})$$

Testing Naïve Bayes

- X_{val} Y_{val} λ $logprior$

$score = predict(X_{val}, \lambda, logprior)$

$pred = score > 0$

$$\frac{1}{m} \sum_{i=1}^m (pred_i == Y_{val_i})$$

$$\begin{bmatrix} 0 \\ 1 \\ 1 \\ \vdots \\ pred_m \end{bmatrix} == \begin{bmatrix} 0 \\ 0 \\ 1 \\ \vdots \\ Y_{val_m} \end{bmatrix}$$

Testing Naïve Bayes

- X_{val} Y_{val} λ \logprior

$score = predict(X_{val}, \lambda, \logprior)$

$pred = score > 0$

$$\frac{1}{m} \sum_{i=1}^m (pred_i == Y_{val_i})$$

$$\begin{bmatrix} 0 \\ 1 \\ 1 \\ \vdots \\ pred_m \end{bmatrix} == \begin{bmatrix} 0 \\ 0 \\ 1 \\ \vdots \\ Y_{val_m} \end{bmatrix}$$
$$\begin{bmatrix} 1 \\ 0 \\ 1 \\ \vdots \\ pred_m == Y_{val_m} \end{bmatrix}$$

Testing Naïve Bayes

- X_{val} Y_{val} λ \logprior

$score = predict(X_{val}, \lambda, \logprior)$

$pred = score > 0$

$$\frac{1}{m} \sum_{i=1}^m (pred_i == Y_{val_i})$$

$$\begin{bmatrix} 0 \\ \underline{1} \\ 1 \\ \vdots \\ pred_m \end{bmatrix} == \begin{bmatrix} 0 \\ \underline{0} \\ 1 \\ \vdots \\ Y_{val_m} \end{bmatrix}$$
$$\begin{bmatrix} 1 \\ 0 \\ \underline{1} \\ \vdots \\ pred_m == Y_{val_m} \end{bmatrix}$$

Testing Naïve Bayes

- X_{val} Y_{val} λ \logprior

$score = predict(X_{val}, \lambda, \logprior)$

$pred = score > 0$

$$\frac{1}{m} \sum_{i=1}^m (pred_i == Y_{val_i})$$

$$\begin{bmatrix} 1 \\ 0 \\ 1 \\ \vdots \\ pred_m == Y_{val_m} \end{bmatrix}$$

Summary

- $X_{val} \ Y_{val} \longrightarrow$ Performance on unseen data
- Predict using λ and *logprior* for each new tweet
- Accuracy $\longrightarrow \frac{1}{m} \sum_{i=1}^m (pred_i == Y_{val_i})$
- What about words that do not appear in $\lambda(\mathbf{w})$?

Applications of Naïve Bayes

$$P(pos|tweet) \approx P(pos)P(tweet|pos)$$

$$P(neg|tweet) \approx P(neg)P(tweet|neg)$$

Applications of Naïve Bayes

$$P(pos|tweet) \approx P(pos)P(tweet|pos)$$

$$P(neg|tweet) \approx P(neg)P(tweet|neg)$$

$$\frac{P(pos|tweet)}{P(neg|tweet)}$$

Applications of Naïve Bayes

Author identification:

$$\frac{P(\text{Shakespeare} | \text{book})}{P(\text{Shakespeare} | \text{book})}$$

Applications of Naïve Bayes

Author identification:

$$\frac{P(\text{Shakespeare}|\text{book})}{P(\text{Lincoln}|\text{book})}$$

Spam filtering:

$$\frac{P(\text{spam}|\text{email})}{P(\text{nospam}|\text{email})}$$

Applications of Naïve Bayes

Word disambiguation:

Bank:



Applications of Naïve Bayes

Word disambiguation:

$$\frac{P(\text{river}|\text{text})}{P(\text{money}|\text{text})}$$

Bank:



Naïve Bayes Applications

- Sentiment analysis
- Author identification
- Information retrieval
- Word disambiguation
- Simple, fast and robust!

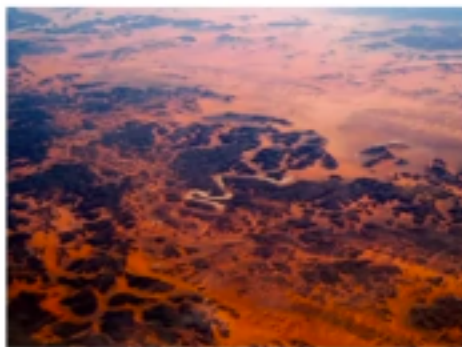
Outline

- Independence
- Relative frequency in corpus

Naïve Bayes Assumptions

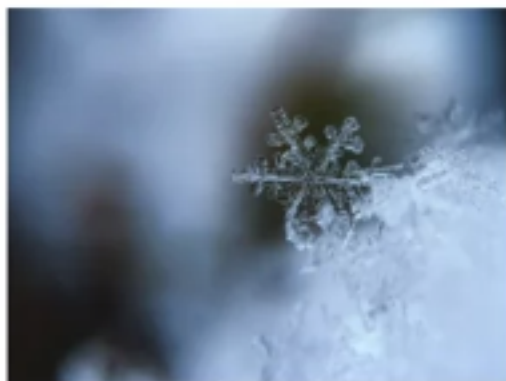
- Independence

“It is sunny and hot in the Sahara desert.”



Naïve Bayes Assumptions

“It’s always cold and snowy in ____.”



spring?? summer? fall?? winter??

Naïve Bayes Assumptions

- Relative frequencies in corpus

Naïve Bayes Assumptions

- Relative frequencies in corpus



Summary

- Independence: Not true in NLP
- Relative frequency of classes affect the model

Outline

- Removing punctuation and stop words
- Word order
- Adversarial attacks

Processing as a Source of Errors: Punctuation

Tweet: My beloved grandmother ✕

processed_tweet: [belov, grandmoth]

Processing as a Source of Errors: Removing Words

Tweet: This is not good, because your attitude is not even close to being nice.

processed_tweet: [good, attitude, close, nice]

Processing as a Source of Errors: Word Order

Tweet: I am happy because I did not go.

Tweet: I am not happy because I did go.

Processing as a Source of Errors: Word Order

Tweet: I am happy because I did not go.



Tweet: I am not happy because I did go.



Processing as a Source of Errors: Word Order

Tweet: I am happy because I did not go.



Tweet: I am not happy because I did go.



Adversarial attacks

Sarcasm, Irony and Euphemisms

Tweet: This is a ridiculously powerful movie. The plot was gripping and I cried right through until the ending!

Adversarial attacks

Sarcasm, Irony and Euphemisms

Tweet: This is a ridiculously powerful movie. The plot was gripping and I cried right through until the ending!

processed_tweet: [ridicul, power, movi, plot, grip, cry, end]